

**Differentiation and integration – 2022 O Level Additional Math****1. June/2022/Paper\_11/No.2**

A particle moves in a straight line such that its displacement,  $s$  metres, from a fixed point, at time  $t$  seconds,  $t \geq 0$ , is given by  $s = (1 + 3t)^{-\frac{1}{2}}$ .

(a) Find the exact speed of the particle when  $t = 1$ . [3]

(b) Show that the acceleration of the particle will never be zero. [2]

**2. June/2022/Paper\_11/No.10**

The normal to the curve  $y = \tan\left(3x + \frac{\pi}{2}\right)$  at the point  $P$  with coordinates  $(p, -1)$ , where  $0 < p \leq \frac{\pi}{6}$ , meets the  $x$ -axis at the point  $A$  and the  $y$ -axis at the point  $B$ . Find the exact coordinates of the mid-point of  $AB$ . [10]

**3. June/2022/Paper\_12/No.7(b)**

- (b) Find  $\int_2^a \frac{8-3x}{(x-1)^2(2x+3)} dx$  where  $a > 2$ . Give your answers in the form  $c + \ln d$ , where  $c$  and  $d$  are functions of  $a$ . [6]

## 4. June/2022/Paper\_12/No.9

The normal to the curve  $y = \frac{\ln(3x^2 + 2)}{x+1}$ , at the point  $A$  on the curve where  $x = 0$ , meets the  $x$ -axis at point  $B$ . Point  $C$  has coordinates  $(0, 3 \ln 2)$ . Find the gradient of the line  $BC$  in terms of  $\ln 2$ . [9]

## 5. June/2022/Paper\_21/No.7

Variables  $x$  and  $y$  are such that  $y = \frac{(1 + \sin 3x)^4}{\sqrt{x}}$ . Use differentiation to find the approximate change in  $y$  when  $x$  increases from 1.9 to  $1.9 + h$ , where  $h$  is small. [6]

## 6. June/2022/Paper\_21/No.10

(a) Differentiate  $x \ln x - 2x$  with respect to  $x$ . Simplify your answer.

[2]

(b) A curve is such that  $\frac{d^2y}{dx^2} = \left(\frac{x+1}{\sqrt{x}}\right)^2$ . It is given that  $\frac{dy}{dx} = \frac{e^2}{2} + 2e$  at the point  $\left(e, \frac{e^3}{6} + e^2\right)$ .

Using your answer to **part (a)**, find the exact equation of the curve.

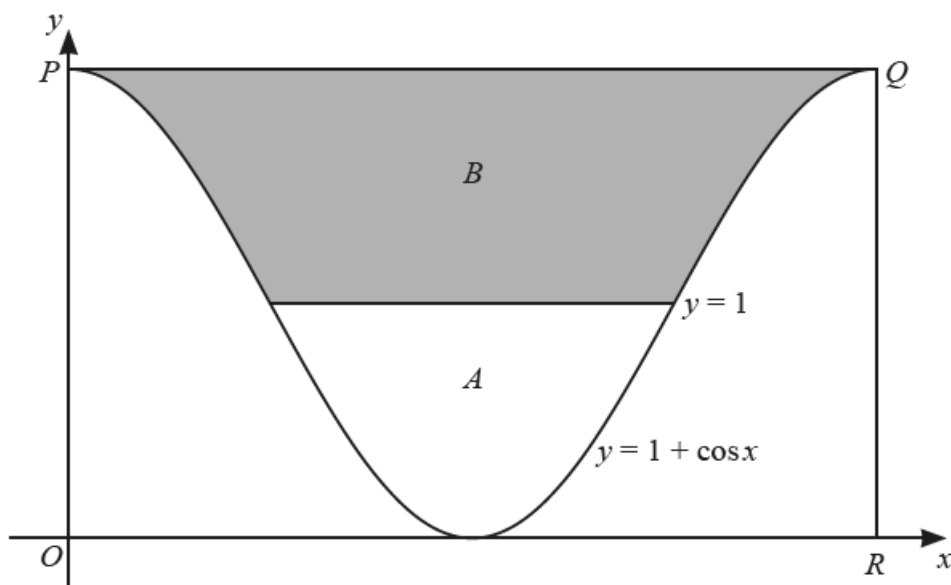
[8]

7. June/2022/Paper\_22/No.7

Differentiate  $y = \frac{e^{4x} \tan x}{\ln x}$  with respect to  $x$ .

[4]

## 8. June/2022/Paper\_22/No.11



The diagram shows part of the line  $y = 1$  and one complete period of the curve  $y = 1 + \cos x$ , where  $x$  is in radians. The line  $PQ$  is a tangent to the curve at  $P$  and at  $Q$ . The line  $QR$  is parallel to the  $y$ -axis. Area  $A$  is enclosed by the line  $y = 1$  and the curve. Area  $B$  is enclosed by the line  $y = 1$ , the line  $PQ$  and the curve.

Given that area  $A$  : area  $B$  is  $1 : k$  find the exact value of  $k$ .

[9]



## 9. June/2022/Paper\_22/No.11

A curve is such that  $\frac{d^2y}{dx^2} = \left(\frac{\sqrt{x} + 1}{\sqrt[4]{x}}\right)^2$ . Given that the gradient of the curve is  $\frac{4}{3}$  at the point  $(1, -1)$ , find the equation of the curve. [7]